

# Particle Kinetics and Dynamics in Flaring Atmospheres Leading to Sunquakes

By

Valentina Zharkova and Serhii Zharkov

**Cambridge**  
**Scholars**  
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This book first published 2025

Cambridge Scholars Publishing

Lady Stephenson Library, Newcastle upon Tyne, NE6 2PA, UK

British Library Cataloguing in Publication Data

A catalogue record for this book is available from the British Library

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ISBN: 978-1-0364-5856-0

ISBN (Ebook): 978-1-0364-5857-7

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